Multi-modal Logics for the Conceptual Analysis of Epistemic Rights

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Logic and Interactive Rationality, June 30, 2022

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- background in logic and in law
- I'm responsible for the Al&Law projects in the Individual and Collective Reasoning (ICR) group in the Interdisciplinary Lab for Intelligent and Adaptive Systems (ILIAS) within the Department of Computer Science

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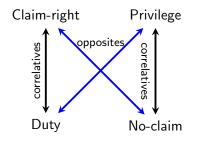
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- these papers: joint work with Olivier Roy (University of Bayreuth)

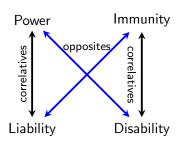
Rights and Duties

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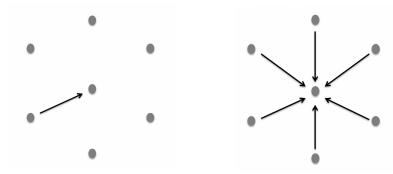
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 recent approaches with agent-based multi-modal logic and DEL: Dong and Roy (2017, 2021), Markovich (2019, 2020)

• normative positions are inherently relational

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- Hohfeld: paucital and multital rights



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- legal language today still uses 'right' to different atomic positions
- sometimes to their molecular combination
- e.g. the freedom of thought consists of:
 - a multital claim-right
 - a multital privilege
 - a multital immunity

Epistemic Rights

- the patient has a right to know the result of her tests, also a right to not know them
- citizens have a right to know that the prime minister has an offshore account
- consumers have a right to not be misled by advertisements
- everyone has a freedom of thought
- the detained person has a right to know his rights

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- our goal: using and developing different formal approaches of epistemic, deontic, and action logics to describe them and to reason with them

Definition – narrow sense

rights that concern the epistemic state of the right-holder (right to know, right to believe, right to explanation, etc.)

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rights that concern the epistemic state of the right-holder (right to know, right to believe, right to explanation, etc.)

Definition – broader sense

also rights that concern the epistemic state of the duty-bearer (right to privacy, right to be forgotten, etc.)

UN Universal Declaration of Human Rights

Article 18: Everyone has the right to freedom of thought, conscience and religion; this right includes freedom to change his religion or belief

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UN Universal Declaration of Human Rights

Article 18: Everyone has the right to freedom of thought, conscience and religion; this right includes freedom to change his religion or belief

Article 19: Everyone has the right to freedom of opinion (...); this right includes freedom to hold opinions without interference (...).

^{*}questions raised by natural law vs. legal positivism

UN's Office of the High Commissioner for Human Rights (OHCHR)

The right to freedom of thought, conscience and religion (which includes the freedom to hold beliefs) in article 18.1 is far-reaching and profound;it encompasses freedom of thought on all matters, personal conviction and the commitment to religion or belief (...). [Article 18] does not permit any limitations whatsoever on the freedom of thought and conscience or on the freedom to have or adopt a religion or belief of one's choice. These freedoms are protected unconditionally, as is the right of everyone to hold opinions without interference in article 19 (...).

UN's Office of the High Commissioner for Human Rights (OHCHR)

The Committee observes that the freedom to "have or to adopt" a religion or belief necessarily entails the freedom to choose a religion or belief, including the right to replace one's current religion or belief with another or to adopt atheistic views, as well as the right to retain one's religion or belief. Article 18 bars coercion that would impair the right to have or adopt a religion or belief, including the use of threat of physical force or penal sanctions to compel believers or non-believers to adhere to their religious beliefs and congregations, to recant their religion or belief or to convert.

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- "protection": multital claim-right against everyone else not to interfere with it
 - is it possible to force someone to believe something? (Orwell's 1984)
 - we don't need to commit, just put it's forbidden

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 - is it possible to force someone to believe something? (Orwell's 1984)
 - we don't need to commit, just put it's forbidden
- "protection": Declaration rules out the possibility of changing this freedom (for example, by a country introducing penal sanctions, that is, duties to accept some specific view): a multital immunity

Language and Semantics

$$p \in \Phi \mid \varphi \wedge \psi \mid \neg \varphi \mid \{ E_{a} \varphi \mid O_{a \to b} \varphi \mid B_{a} \varphi \}_{a,b \in A} \mid \Box \varphi$$

$$\mathfrak{F} = \langle W, \{f_a, R_{a,b}^O, R_a^B\}_{a,b \in A} \rangle$$

- $\bullet \mathcal{M}, w \models E_a \varphi \Leftrightarrow ||\varphi|| \in f_a(w)$
- $\mathcal{M}, w \models \mathbf{0}_{a \to b} \varphi \Leftrightarrow \forall w'(wR_{a,b}^O w' \Rightarrow \mathcal{M}, w' \models \varphi)$
- $\bullet \ \mathcal{M}, w \models \mathbf{B}_{\mathsf{a}} \varphi \Leftrightarrow \forall w' (w R^{B}_{\mathsf{a}} w' \Rightarrow \mathcal{M}, w' \models \varphi)$
- $\bullet \ \mathcal{M}, w \models \Box \varphi \Leftrightarrow \forall w', \mathcal{M}, w' \models \varphi$

Freedom of Thought: Privilege

$$\bigwedge_{b \in A} P_{a \to b} \mathbf{B}_{a} \phi \qquad (\text{FoT-F-} B_{a} \phi)$$

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$$\bigwedge_{\cdot} (P_{a \to b} \mathbf{B}_{a} \phi \wedge P_{a \to b} \mathbf{B}_{a} \neg \phi \wedge P_{a \to b} (\langle \mathbf{B}_{a} \rangle \phi \wedge \langle \mathbf{B}_{a} \rangle \neg \phi)) \text{ (FoT-F-} a-\phi)$$

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$$\bigwedge_{b \in A} \mathbf{O}_{b \to a} (\neg E_b \neg E_a B_a \phi \wedge \neg E_b \neg E_a B_a \neg \phi \wedge \neg E_b \neg E_a (\langle B_a \rangle \phi \wedge \langle B_a \rangle \neg \phi))$$

 $(FoT-C-a-\phi)$

Freedom of Thought: Immunity

$$\bigwedge_{b \in A} \neg \Diamond (E_b(\neg(\mathsf{FoT}\text{-}\mathsf{F-}\mathsf{a-}\phi)) \vee E_b(\neg(\mathsf{FoT}\text{-}\mathsf{C-}\mathsf{a-}\phi))) \qquad (\mathsf{FoT}\text{-}\mathsf{I-}\mathsf{a-}\phi)$$

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$$\mu x. \bigwedge_{b \in A} \neg \Diamond (E_b \neg (\mathsf{FoT-F-}a-\phi) \lor E_b \neg (\mathsf{FoT-C-}a-\phi) \lor E_b \neg x)$$

Freedom of Thought

$$(FoT-F-a-\phi) \wedge (FoT-C-a-\phi) \wedge (FoT-I-a-\phi)$$
 (FoT-a- ϕ)

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 Even a power?

Right to Know

Right to Know

Claim-right? Power? Privilege? Immunity?

The citizens have a right to know the MPs' declarations of property—this is a claim-right

The citizens have a right to know the local representatives' declarations of property—this is a power

Right to Know as a Claim-right

Texas Senate Bill 25

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Right to know whether

the expectant parents have a right to know whether the fetus is ill (whether it would be a healthy child)

Language and Semantics

$$p \in \Phi \mid \phi \land \psi \mid \neg \phi \mid \mathbf{K}_{\mathsf{a}} \phi \mid \mathbf{O}_{\mathsf{a} \to \mathsf{b}} (\phi / \psi) \mid E_{\mathsf{a}} \phi \mid \Box \phi$$

$$\mathfrak{F} = \langle W, \{R_a, \leq_{a \to b}, f_a\}_{a,b \in A}, R_{\square} \rangle$$

- \mathfrak{M} , $w \models E_a \varphi \Leftrightarrow ||\phi|| \in f_a(w)$.
- $\mathfrak{M}, w \models \Box \varphi \Leftrightarrow \forall v \text{ such that } wR_{\Box}v, \mathfrak{M}, v \models \varphi$
- $\mathfrak{M}, w \models K_{\mathsf{a}}\varphi \Leftrightarrow \forall v \text{ such that } wR_{\mathsf{a}}v, \mathfrak{M}, v \models \varphi$
- $\mathfrak{M}, w \models \mathbf{O}_{a \to b}(\varphi/\psi) \Leftrightarrow \forall v \in \max_{\leq_{a \to b}}(||\psi|| \cap R_{\square}[w]), \mathfrak{M}, v \models \varphi$

Dynamic Modalities

Given a set of indexes I, an action model A_a for agent a is a tuple

$$\langle A, \{R_i\}_{i \in I}, Pre \rangle$$

- A is a non-empty, finite set of actions.
- Each R_i is binary relation on A.
- $Pre: A \rightarrow \mathcal{L}$ is a precondition function.

$$\mathfrak{M}, w \models [\mathcal{A}_i, a] \phi$$
 iff if $\mathfrak{M}, w \models Pre(a)$ then $\mathfrak{M}' \otimes \mathcal{A}_i, (w, a) \models \phi$

Where $\mathfrak{M}' \otimes \mathcal{A}_i$ is obtained by product update on the relevant relations.

Right to Know as a (Conditional) Claim-right

Right to know whether:

• Static (KWS):

$$\mathbf{O}_{d \to p} E_d(\mathbf{K}_p(ill) \lor \mathbf{K}_p(\neg ill))$$

Dynamic (KWD):

$$\mathbf{O}_{d
ightarrow
ho} igwedge_{a \in \mathcal{A}_d} [\mathcal{A}_d, a] (\mathbf{K}_
ho(\mathit{ill}) ee \mathbf{K}_
ho(\lnot\mathit{ill}))$$

Right to Know as a (Conditional) Claim-right

Pairs of conditional obligations:

• Static (COS):

$$\mathbf{O}_{d o p}(E_d \mathbf{K}_p(ill)/ill) \wedge \mathbf{O}_{d o p}(E_d \mathbf{K}_p(\neg ill)/\neg ill)$$

Dynamic (COD):

$$\mathbf{O}_{d \to p}(\bigwedge_{a \in \mathcal{A}_d} [\mathcal{A}_d, a] \mathbf{K}_p(ill)/ill) \wedge \mathbf{O}_{d \to p}(\bigwedge_{a \in \mathcal{A}_d} [\mathcal{A}_d, a] \mathbf{K}_p(\neg ill)/\neg ill)$$

Right to Know as a (Conditional) Claim-right

Pair of wide-scope conditionals:

• Static (WSS):

$$\mathbf{O}_{d \to p}(ill \to E_d \mathbf{K}_p(ill)) \wedge \mathbf{O}_{d \to p}(\neg ill \to E_d \mathbf{K}_p(\neg ill))$$

Dynamic (WSD):

$$\mathbf{O}_{d \to p}(\mathit{ill} \to \bigwedge_{a \in \mathcal{A}_d} [\mathcal{A}_d, a] \mathbf{K}_p(\mathit{ill})) \wedge \mathbf{O}_{d \to p}(\neg \mathit{ill} \to \bigwedge_{a \in \mathcal{A}_d} [\mathcal{A}_d, a] \mathbf{K}_p(\neg \mathit{ill}))$$

Logical Relationships

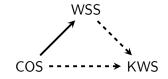


Figure 1: Static formalizations

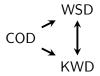


Figure 2: Dynamic formalizations

Further Questions

• Detachment Principles (factual, necessary, deontic).

Aqvist Paradox.

Right to know as a power.

Relationship between a claim-right and a power

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x bears an obligation to y that F under the system N of norms iff in the case that F is not true then y has the power under the code N to initiate legal action against x for non-fulfillment of F

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the right-to-left direction of the biconditional does not work Markovich (2020): power shouldn't be in the definition of claim-right

What is the relation between a claim-right and a power then?

Power to initiate a legal action: possibility to put a duty on the judiciary to settle whether what is put in the cause of action holds

Power to initiate a legal action: possibility to put a duty on the judiciary to settle whether what is put in the cause of action holds 'wrongful birth': failing to warn the parents about the illness

Power to initiate a legal action: possibility to put a duty on the judiciary to settle whether what is put in the cause of action holds 'wrongful birth': failing to warn the parents about the illness no such cause of action \rightarrow no possibility to sue \rightarrow no claim-right?

Language and Semantics

$$p \in \Phi \mid \phi \land \psi \mid \neg \phi \mid \mathbf{K}_{\mathsf{a}} \phi \mid \mathbf{O}_{\mathsf{a} \to \mathsf{b}} (\phi / \psi) \mid E_{\mathsf{a}} \phi \mid \Box \phi$$

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Right to know

$$\mathbf{O}_{d \rightarrow p}(E_d \mathbf{K}_p(ill) / K_d(ill)) \wedge \mathbf{O}_{d \rightarrow p}(E_d \mathbf{K}_p(\neg ill) / K_d(\neg ill))$$

Abbreviated as:

$$\mathbf{O}_{d \to p}(E_d \mathbf{K}_p(\pm iII)/K_d \pm iII)$$

Legal action

Positive case:

$$E_j(\Box \neg E_d(KW_p(iII)))$$

Negative case:

$$E_{j}(\Box(\Diamond E_{d}(KW_{p}(iII)) \land \Diamond \neg E_{d}(KW_{p}(iII))))$$

Together:

$$E_{j}(\Box \neg E_{d}(KW_{p}(ill)) \lor E_{j}(\Box (\Diamond E_{d}(KW_{p}(ill)) \land \Diamond \neg E_{d}(KW_{p}(ill))))$$
(LA)

Power to initiate legal action

$$\Diamond E_p(O_{j\to p}(LA))$$

Power as necessary condition for claim-right

$$\mathbf{O}_{d o p}(E_d \mathbf{K}_p(\pm i II)/K_d \pm i II) o \Diamond E_p(O_{j o p}(LA))$$

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Conclusion

- Theory of normative positions is well established and understood.
- Epistemic rights had not been studied so far in that theory.
- Simple extension of the theory of normative positions allows to express complex epistemic rights, study their logical relationships and behavior.
- Next steps:
 - Recursive elements in protected liberties.
 - Alternative formalization of conditional duties for better detachment principles.
 - Mathematical characterization of the frame conditions corresponding to the constraint imposed by the Bill 25.
 - Other epistemic rights.

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